



US009473115B2

(12) **United States Patent**
Raj et al.

(10) **Patent No.:** **US 9,473,115 B2**
(45) **Date of Patent:** ***Oct. 18, 2016**

(54) **QUADRATURE-BASED INJECTION
LOCKING OF RING OSCILLATORS**

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(*) Notice: Subject to any disclaimer, the term of this
patent is extended or adjusted under 35
U.S.C. 154(b) by 0 days.

This patent is subject to a terminal dis-
claimer.

(21) Appl. No.: **14/944,925**

(22) Filed: **Nov. 18, 2015**

(65) **Prior Publication Data**

US 2016/0079966 A1 Mar. 17, 2016

Related U.S. Application Data

(63) Continuation of application No. 14/479,269, filed on
Sep. 5, 2014, now Pat. No. 9,219,486.

(60) Provisional application No. 61/905,660, filed on Nov.
18, 2013.

(51) **Int. Cl.**
H03B 27/00 (2006.01)
H03K 3/03 (2006.01)
H03L 7/099 (2006.01)
H03L 7/24 (2006.01)

(52) **U.S. Cl.**
CPC **H03K 3/0315** (2013.01); **H03B 27/00**
(2013.01); **H03L 7/0995** (2013.01); **H03L 7/24**
(2013.01); **H03B 2201/038** (2013.01)

(58) **Field of Classification Search**

CPC H03B 27/00; H03B 2201/038; H03K
3/0315; H03K 3/0322; H03L 7/0995

USPC 331/45, 57, 185, 186
See application file for complete search history.

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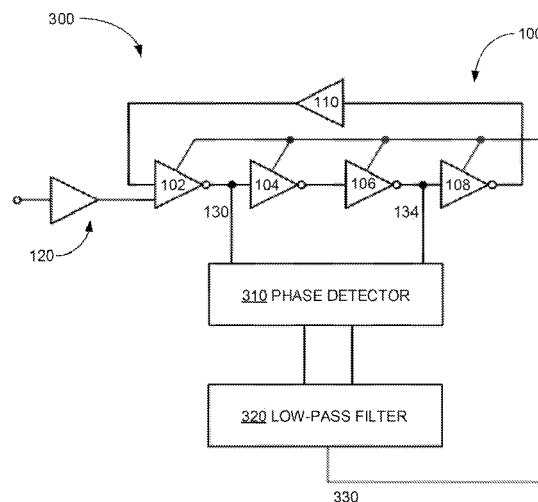
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(57) **ABSTRACT**

Technologies are generally described for quadrature-based
injection-locking of ring oscillators. In some examples, an
external signal may be injected into a ring oscillator. Phase
signals may be measured from within the ring oscillator and
used to determine a mean quadrature error (MQE) that
characterizes the difference in frequency between the exter-
nal signal and the ring oscillator's natural frequency. A
control signal may then be generated from the MQE and
used to adjust the ring oscillator natural frequency to reduce
the difference between the ring oscillator natural frequency
and the external signal.

20 Claims, 9 Drawing Sheets



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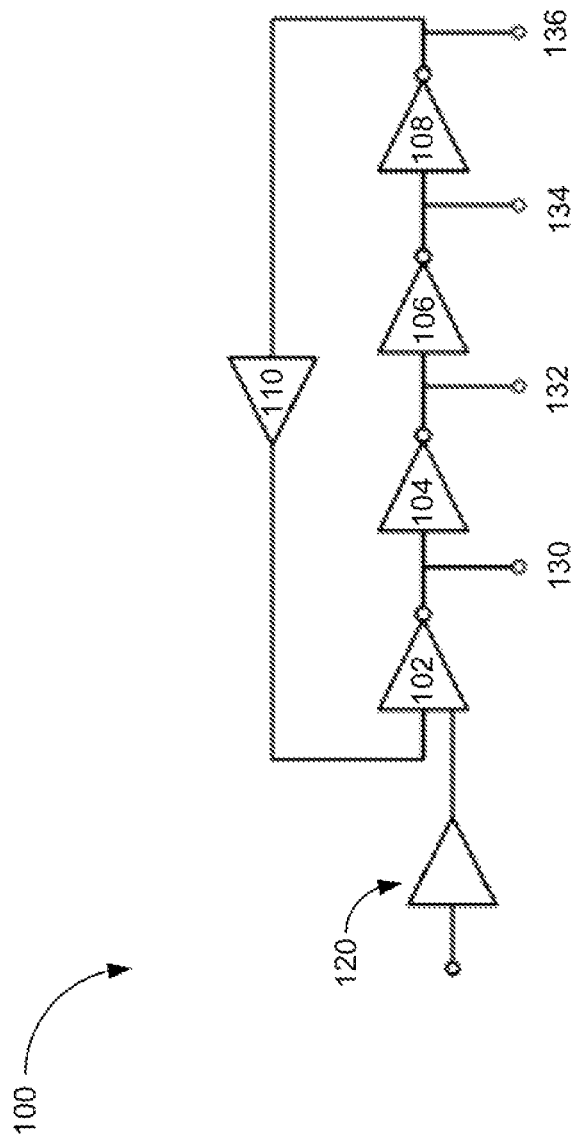


FIG. 1

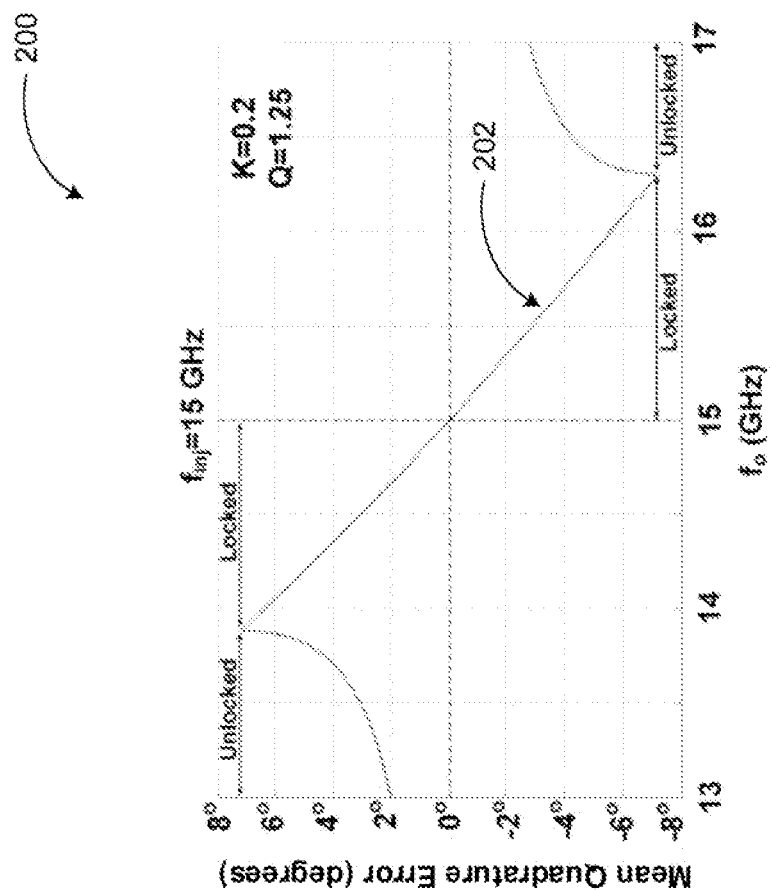


FIG. 2

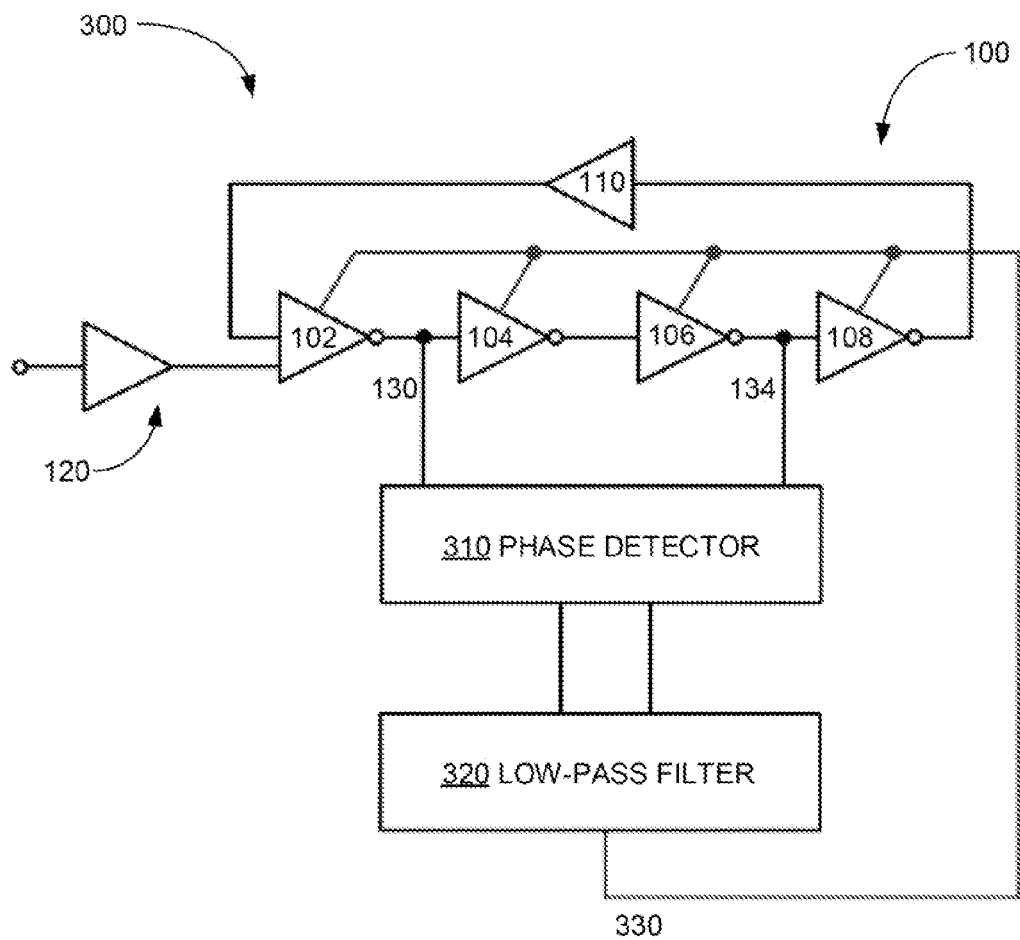


FIG. 3

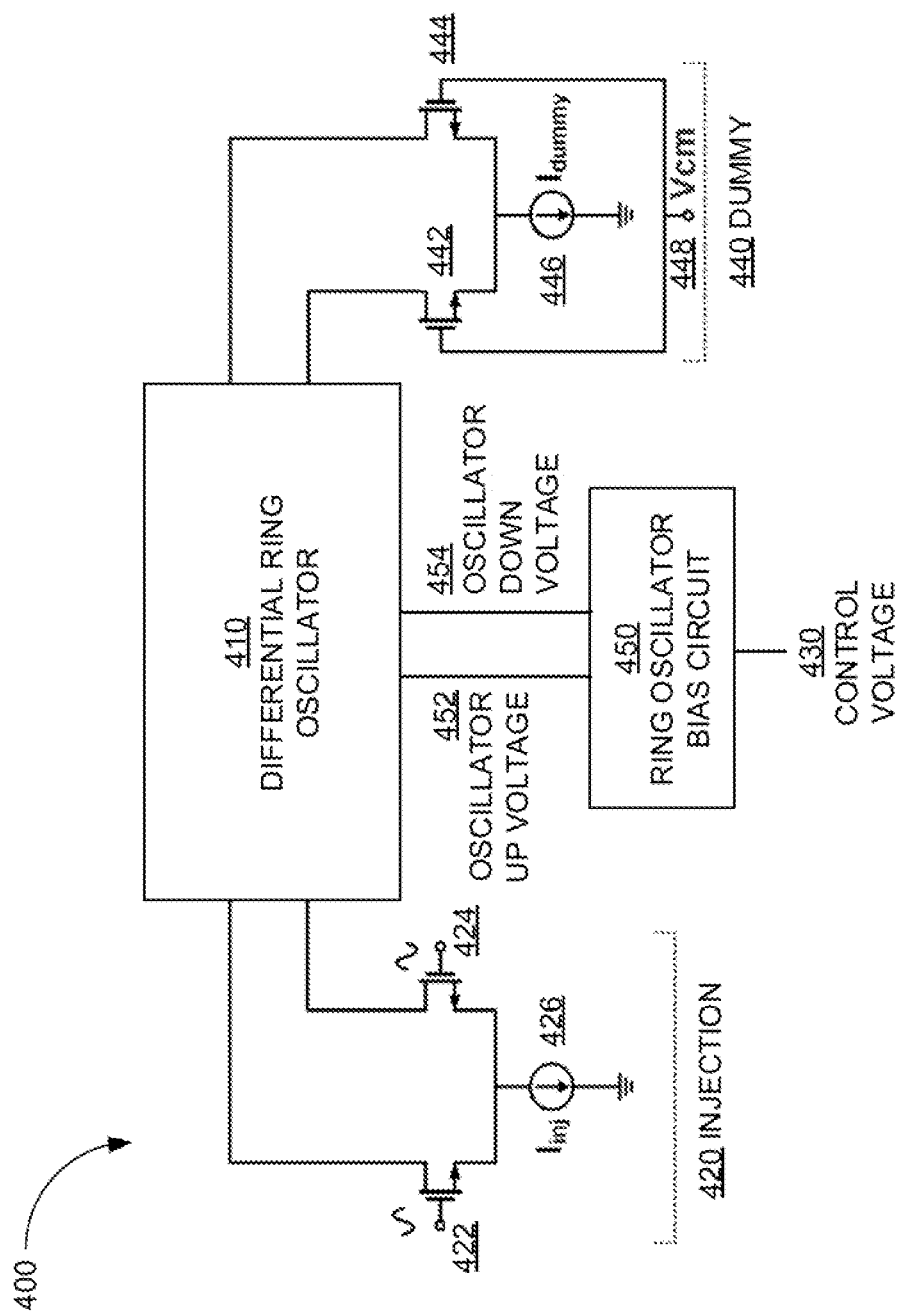


FIG. 4

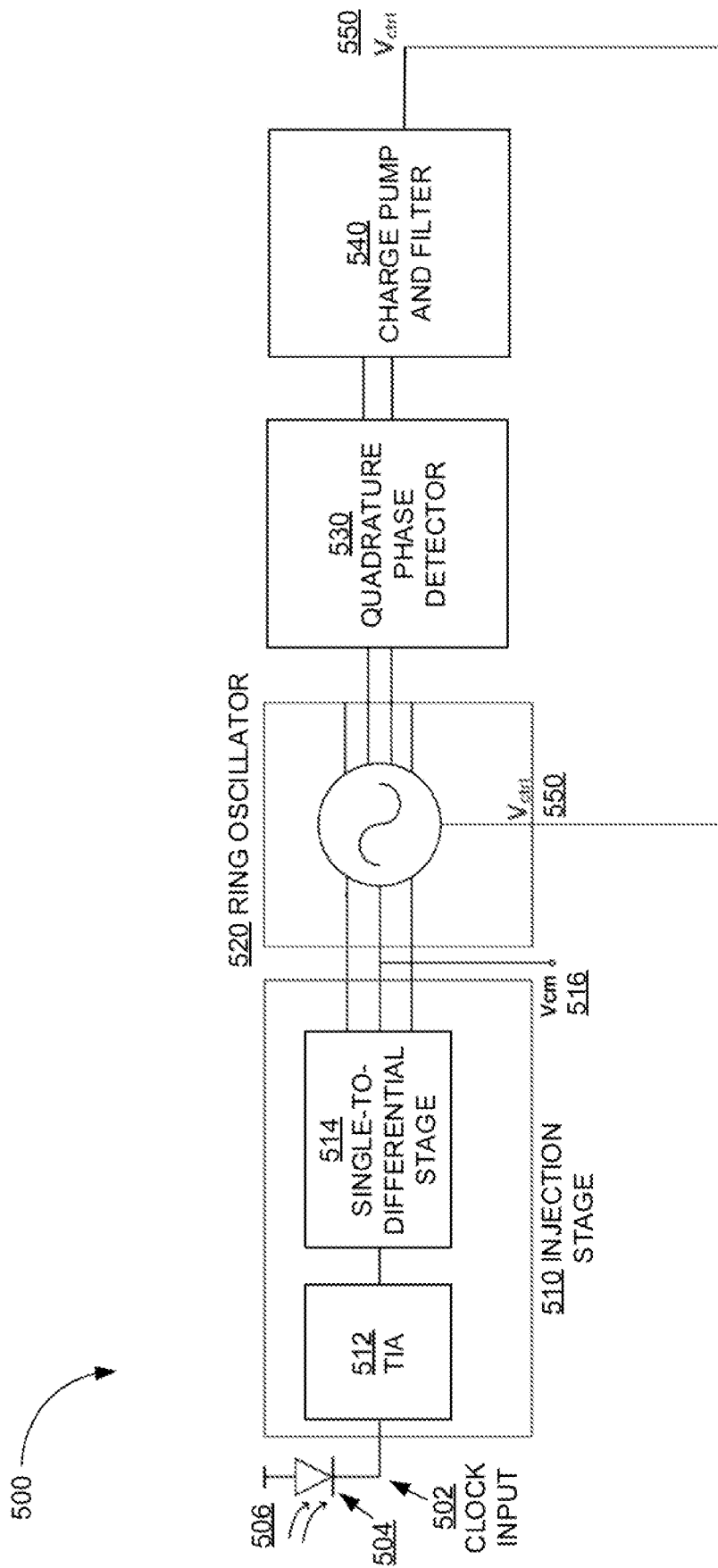


FIG. 5

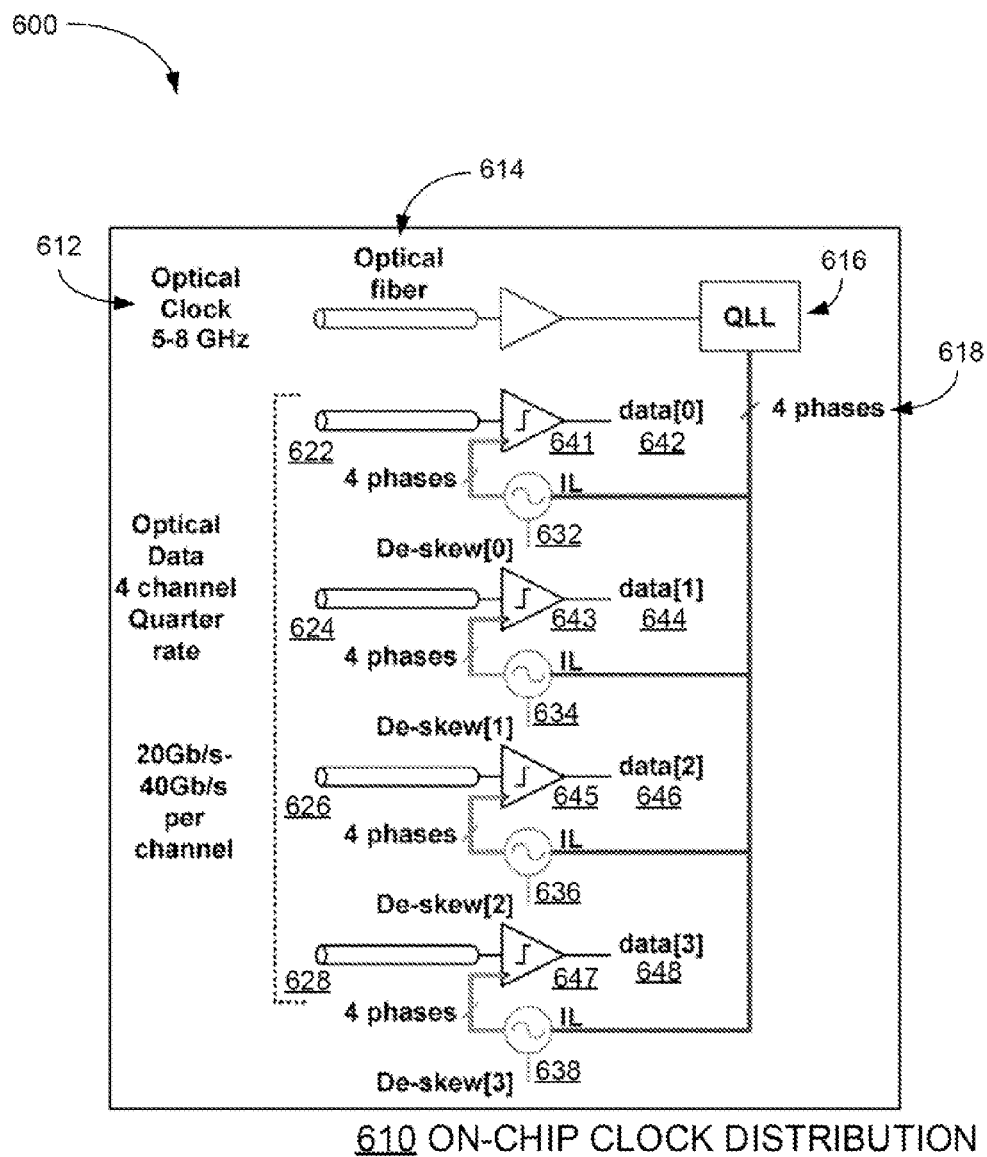


FIG. 6

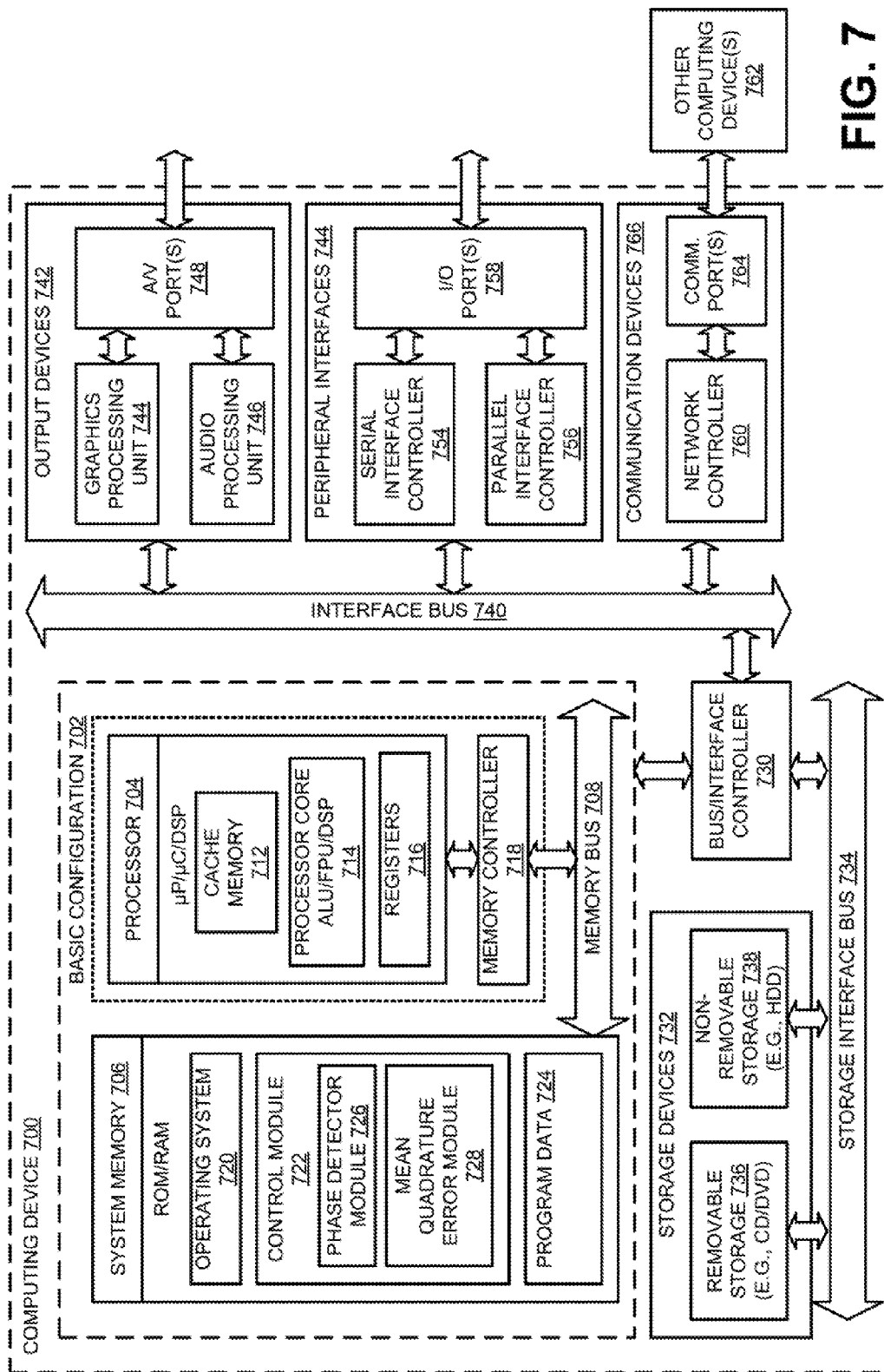


FIG. 7

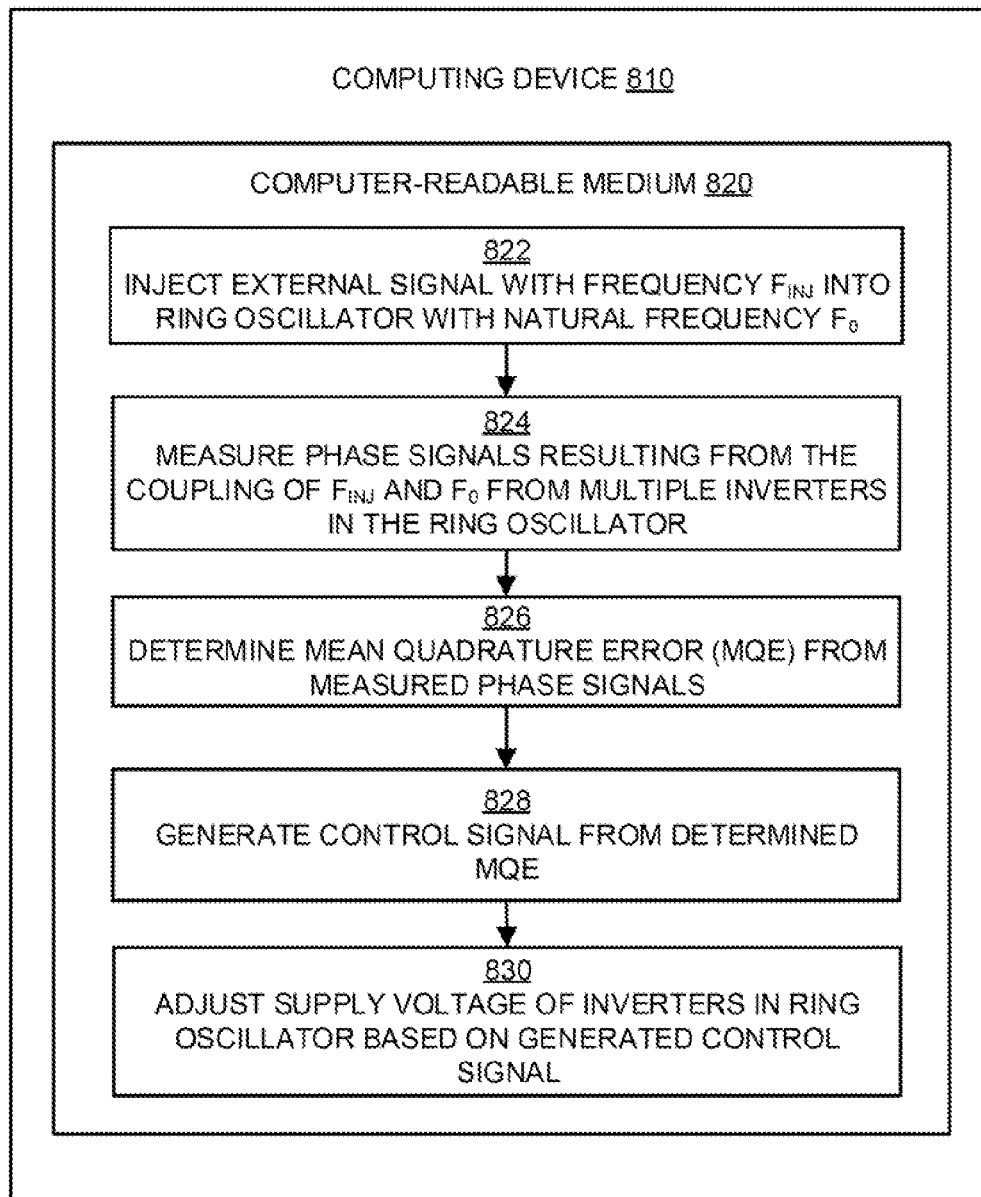


FIG. 8

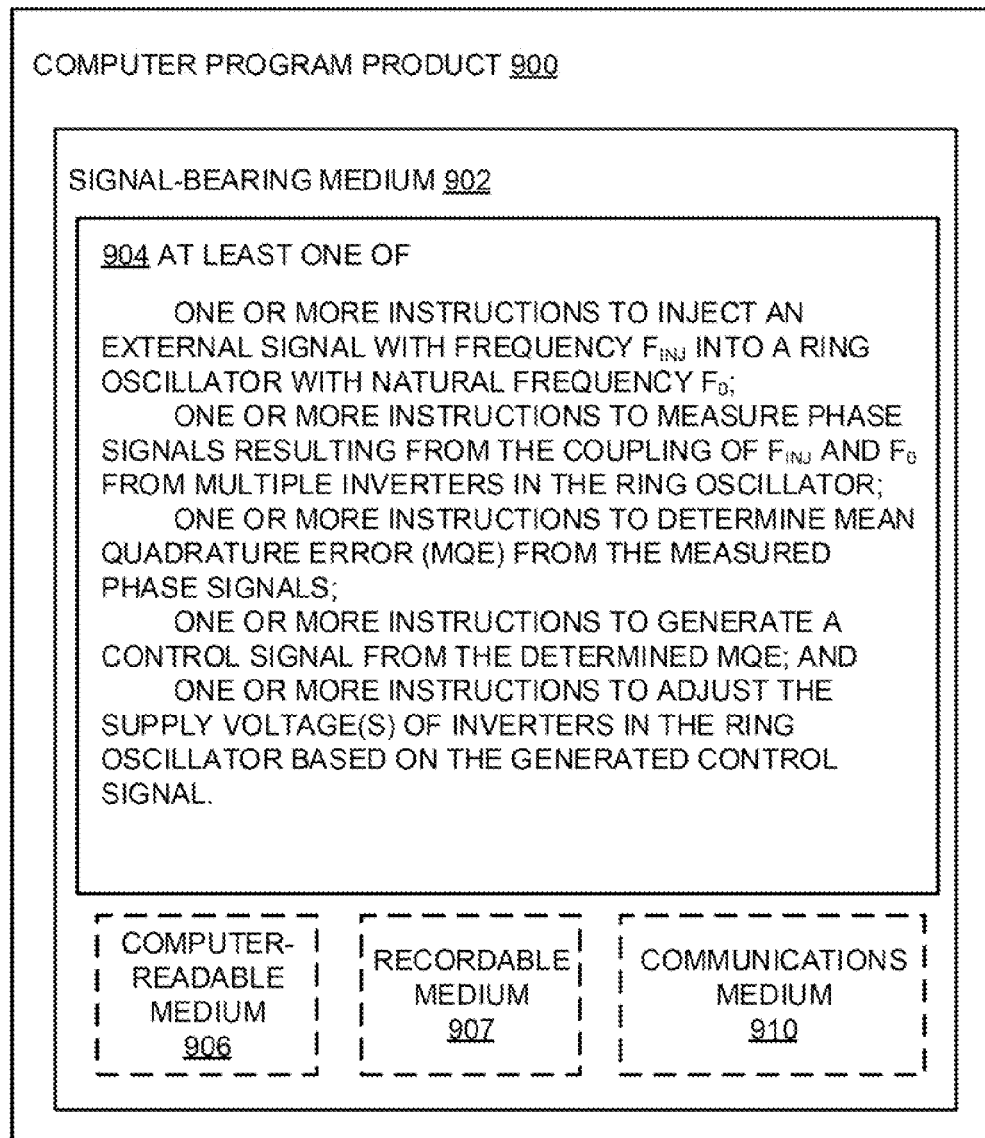


FIG. 9

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QUADRATURE-BASED INJECTION LOCKING OF RING OSCILLATORS

CROSS-REFERENCE TO RELATED APPLICATIONS

This application is a continuation under 35 U.S.C. §120 of U.S. patent application Ser. No. 14/479,269 filed on Sep. 5, 2014 and patented as U.S. Pat. No. 9,219,486 on Dec. 22, 2015, which in turn claims priority under 35 U.S.C. §119(e) as a non-provisional application of U.S. Provisional Patent Application Ser. No. 61/905,660 filed on Nov. 18, 2013, entitled “Quadrature Locked Loop (QLL)”. The disclosures of the U.S. patent and the U.S. Provisional Patent Application are hereby incorporated by reference in their entireties.

BACKGROUND

Unless otherwise indicated herein, the materials described in this section are not prior art to the claims in this application and are not admitted to be prior art by inclusion in this section.

Ring oscillators may include inverter-based circuits that may be used to generate clock signals for other circuit blocks. A ring oscillator may be implemented using an odd number of inverters coupled in series, with the output terminal of the last inverter coupled to the input terminal of the first inverter. An inverter outputs a signal that is opposite in sign to its input, and may do so for a finite period of time after the input is applied. Accordingly, the output of an inverter in a ring oscillator may switch signs with a particular frequency, thereby providing a clock signal suitable for other circuit blocks.

SUMMARY

The present disclosure generally describes techniques to injection-lock ring oscillators.

According to some examples, methods are described to injection-lock a ring oscillator having multiple inverters and a natural frequency. Example methods may include injecting an external signal with an injection frequency into the multiple inverters, detecting a first phase signal, formed from a coupling of the natural frequency and the injection frequency, from a first inverter in the multiple inverters. The methods may also include detecting a second phase signal, formed from the coupling of the natural frequency and the injection frequency, from a second inverter in the multiple inverters, determining a mean quadrature error (MQE) from at least the first phase signal and the second phase signal. The methods may further include generating a control signal from the determined MQE and adjusting the natural frequency of the ring oscillator based on the control signal.

According to other examples, injection-locked ring-oscillator systems are described. Example systems may include multiple inverters, a phase detector module coupled to the multiple inverters, and a control module coupled to the phase detector module. The inverters may be configured to receive an external signal with an injection frequency and to output an oscillation signal. The phase detector module may be configured to detect a first phase signal, formed from a coupling of a natural frequency of the system and the injection frequency, from a first inverter in the multiple inverters and to detect a second phase signal, formed from the coupling of the natural frequency of the system and the injection frequency from a second inverter in the multiple inverters. The phase detector module may also be configured

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to determine a mean quadrature error (MQE) from at least the first phase signal and the second phase signal. The control module may be configured to generate a control signal from the determined MQE and adjust a supply voltage to at least one of the multiple inverters based on the control signal.

According to further examples, a clock signal distribution circuit is provided. The circuit may include a clock signal injection stage, a ring oscillator with a natural frequency and coupled to the clock signal injection stage, a quadrature phase detector module coupled to the ring oscillator, and a low-pass filter module coupled to the ring oscillator and the quadrature phase detector module. The clock signal injection stage may be configured to receive a clock signal and use the clock signal to output an injection signal with an injection frequency. The ring oscillator may be configured to receive the injection signal and output multiple oscillation signals. The quadrature phase detector module may be configured to detect, from the ring oscillator, multiple phase signals formed from the coupling of the natural frequency and the injection frequency, and determine a mean quadrature error (MQE) from the multiple phase signals. The low-pass filter module may be configured to generate a control signal from the determined MQE and provide the control signal to the ring oscillator.

The foregoing summary is illustrative only and is not intended to be in any way limiting. In addition to the illustrative aspects, embodiments, and features described above, further aspects, embodiments, and features will become apparent by reference to the drawings and the following detailed description.

BRIEF DESCRIPTION OF THE DRAWINGS

The foregoing and other features of this disclosure will become more fully apparent from the following description and appended claims, taken in conjunction with the accompanying drawings. Understanding that these drawings depict only several embodiments in accordance with the disclosure and are, therefore, not to be considered limiting of its scope, the disclosure will be described with additional specificity and detail through use of the accompanying drawings, in which:

FIG. 1 illustrates an example ring oscillator;

FIG. 2 illustrates a diagram of an example of mean quadrature error versus frequency difference in a ring oscillator system;

FIG. 3 illustrates an example ring oscillator system that may implement quadrature-based injection locking;

FIG. 4 illustrates a detailed diagram of an example ring oscillator system that may be controlled using quadrature-based injection locking;

FIG. 5 illustrates a detailed diagram of an example ring oscillator system that may implement quadrature-based injection locking;

FIG. 6 illustrates an example on-chip clock distribution system that may use quadrature-based injection locking;

FIG. 7 illustrates a general purpose computing device that could be used in conjunction with a ring, oscillator that implements quadrature-based injection-locking;

FIG. 8 is a flow diagram illustrating an example method to perform quadrature-based injection-locking of a ring oscillator that may be performed by a computing device such as the computing device in FIG. 7; and

FIG. 9 illustrates a block diagram of an example computer program product, all arranged in accordance with at least some embodiments described herein.

DETAILED DESCRIPTION

In the following detailed description, reference is made to the accompanying drawings, which form a part hereof. In the drawings, similar symbols typically identify similar components, unless context dictates otherwise. The illustrative embodiments described in the detailed description, drawings, and claims are not meant to be limiting. Other embodiments may be utilized, and other changes may be made, without departing from the spirit or scope of the subject matter presented herein. The aspects of the present disclosure, as generally described herein, and illustrated in the Figures, can be arranged, substituted, combined, separated, and designed in a wide variety of different configurations, all of which are explicitly contemplated herein.

This disclosure is generally drawn, inter alia, to methods, apparatus, systems, devices, and/or computer program products related to quadrature-based injection-locking of ring oscillators.

Briefly stated, technologies are generally described for quadrature-based injection-locking of ring oscillators. In some examples, an external signal may be injected into a ring oscillator. Phase signals may be measured from within the ring oscillator and used to determine a mean quadrature error (MQE) that characterizes a difference in frequency between the external signal and the ring oscillator's natural frequency. A control signal may then be generated from the MQE and used to adjust the ring oscillator natural frequency to reduce the difference between the ring oscillator natural frequency and the external signal.

FIG. 1 illustrates an example ring oscillator **100** arranged in accordance with at least some embodiments described herein.

The ring oscillator **100** may include inverters **102**, **104**, **106** and **108** with an additional inverter stage **110**. The ring oscillator **100** may be configured to output a number of output oscillation signals **130**, **132**, **134** and **136**, which oscillate and which correspond to the outputs of the inverters **102**, **104**, **106** and **108** respectively. The ring oscillator **100** may also include an external signal **120** (provided via one or more signal sources) that may be injected into the ring oscillator **100** as an input to the inverter **102**.

As described above, a ring oscillator may be implemented with an odd number of inverter stages coupled in series. For example, the inverters **102**, **104**, **106** and **108** may be coupled in series, with the output terminal of each inverter coupled to the input terminal of another inverter. The inverter stage **110** may be implemented as an inverter or may be implemented by some other circuit configured to invert an input signal. In some embodiments, the inverter stage **110** may be configured to operate significantly faster than the inverters **102-108** so as to reduce its effect on the oscillation timing of the ring oscillator **100**. During operation of the ring oscillator **100**, the output oscillation signals **130-136** output from the inverters **102-108** may oscillate at the same frequency but differ in phase. For example, the output signal **132** may oscillate at the same frequency as the output signal **130**, but have a phase that lags the phase of the output signal **130** due to signal delay from the inverter **104**. In the absence of external signals, the output oscillation signals **130-136** may oscillate at a natural frequency of the ring oscillator **100**, which may be based on the structure of the inverters **102-110** and the power (in terms of voltage and/or current)

supplied to the inverters **102-110** and/or based on some other factor(s) or combination(s) thereof.

While the ring oscillator **100** is depicted as including five inverter stages, in other embodiments, a ring oscillator may include more inverter stages or fewer inverter stages. The number of inverter stages may be selected based on a target natural frequency of the ring oscillator, a target number of potential output oscillation signals, or any other suitable criteria.

In some embodiments, the ring oscillator **100** may be used to provide output signals that are synchronized to an external signal. For example, the external signal **120** may be a clock signal, and the ring oscillator **100** may attempt to synchronize the output oscillation signals **130-136** to the frequency of the external signal **120**. As a result, the output oscillation signals **130-136** may oscillate at the frequency of the external signal **120**. However, if the frequency of the external signal **120** does not match the natural frequency of the ring oscillator **100** then phase errors may arise in the output oscillation signals **130-136** in some embodiments, quadrature-based injection locking may be used to reduce the phase errors in ring oscillator output signals by reducing the difference between the frequency of an external signal and the natural frequency of the ring oscillator.

FIG. 2 illustrates a diagram of an example of mean quadrature error versus frequency difference in a ring oscillator system, arranged in accordance with at least some embodiments described herein.

As shown in the diagram **200**, a mean quadrature error (MQE) curve **202** may vary based on the difference between the natural frequency of a ring oscillator (denoted by f_0) and the frequency of an externally injected signal (denoted by f_{inj}). In some embodiments, the MQE may be the average quadrature phase error (for example, the phase difference between two signals that are nominally offset by 90° in phase), and may be determined by:

$$MQE = \frac{\pi}{2} \left(\frac{\omega_{inj}}{\omega_0} + \frac{\omega_b}{\omega_0} - 1 \right)$$

where

$$\omega_b = \sqrt{(\omega_0 - \omega_{inj})^2 - \omega_l^2}$$

$$\omega_l = \frac{\omega_0}{2Q}k$$

$$\omega_{inj} = 2\pi f_{inj}, \text{ and } \omega_0 = 2\pi f_0.$$

As shown by the MQE curve **202**, the magnitude (for example, absolute value) of the MQE may vary according to the difference between f_0 and f_{inj} during the locked state, (for example, when $(\omega_0 - \omega_{inj})^2 < \omega_l^2$). For example, as f_0 grows larger than f_{inj} in the locked state, the MQE may become more and more negative (for example, larger in absolute value while remaining negative). Similarly, as f_0 becomes smaller than f_{inj} in the locked state, the MQE may become more and more positive (for example, larger in absolute value while remaining positive). Accordingly, the magnitude and sign of a measured MQE value may be used to match f_0 to f_{inj} . For example, f_0 may be reduced in response to determining that the measured MQE value is negative and the system is locked. Similarly, f_0 may be increased in response to determining that the measured MQE value is positive and the system is locked. In either case, the adjustment of f_0 may continue until the measured MQE value is substantially zero (for example, until f_0 substantially equals f_{inj}), thereby reducing phase error in the outputs of the ring

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oscillator. In situations where a ring oscillator system begins in the unlocked state, where $(\omega_0 - \omega_{inj})^2 \geq \omega_L^2$, the natural frequency f_0 and/or the injection frequency f_{inj} may be adjusted via other suitable technique until the system is locked.

FIG. 3 illustrates an example ring oscillator system that may implement quadrature-based injection locking, arranged in accordance with at least some embodiments described herein.

As depicted in a ring oscillator system 300, the ring oscillator 100 which may be arranged to provide quadrature output oscillation signals, may be coupled to a phase detector 310, which in turn may be coupled to a low-pass filter 320 that may output a control signal 330. The phase detector 310 may be configured to determine the MQE as described above. The phase detector 310 may be coupled to receive two quadrature output oscillation signals that are nominally offset by 90° in phase. For example, the phase detector 310 may be coupled to the output terminals of the inverters 102 and 106 so as to receive output oscillation signals 130 and 134, respectively originating from the inverters 102 and 106, which may be separated by the inverter 104. In some embodiments, the phase detector 310 may instead be coupled to the output terminals of the inverters 104 and 108 respectively corresponding to the output oscillation signals 132 and 136.

The phase detector 310 may in turn be configured to output the determined MQE to the low-pass filter 320. The low-pass filter 320 may be configured to reduce or remove high-frequency variations in the MQE received from the phase detector 310 and output a relatively low-frequency signal that may be proportional (for example) to the difference between the phases of the output oscillation signals 130 and 134. The low-frequency signal output by the low-pass filter 320 may then be used as the control signal 330 to adjust the natural frequency f_0 of the ring oscillator 100 to reduce the magnitude of the determined MQE (which may be representative of the frequency difference between f_0 and f_{inj}).

In some embodiments, the control signal 330 may be directly used as the supply voltage for the inverters 102-108 of the ring oscillator 100. For example, in response to the determination of a positive MQE (for example, $f_0 < f_{inj}$) by the phase detector 310, the low-pass filter 320 may increase the magnitude of the control signal 330 and therefore increase the supply voltage to the inverters 102-108. The increase in supply voltage may result in an increase in operating speed for the inverters 102-108, causing the ring oscillator 100 to oscillate faster and thereby increase f_0 . As another example, in response to the determination of a negative MQE (for example, $f_0 > f_{inj}$) by the phase detector 310, the low-pass filter 320 may decrease the magnitude of the control signal 330 and therefore decrease the supply voltage to the inverters 102-108. The decrease in supply voltage may result in a decrease in operating speed for the inverters 102-108, causing the ring oscillator 100 to oscillate slower and thereby decrease f_0 . In either case, as f_0 approaches f_{inj} , the magnitude of the determined MQE may decrease until f_0 substantially matches f_{inj} .

FIG. 4 illustrates a detailed diagram of an example ring oscillator system that may be controlled using quadrature-based injection locking, arranged in accordance with at least some embodiments described herein.

In some embodiments, a ring oscillator system 400 may be implemented as a differential system to improve noise rejection. The ring oscillator system 400 may include an injection section 420 and a dummy section 440, both

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coupled to a differential ring oscillator 410. The injection section 420 may include a transistor 422 and a transistor 424, both coupled to an injection current source 426. The dummy section 440 may include a transistor 442 and a transistor 444, both coupled to a dummy current source 446 and having gates coupled to a common mode voltage 448. The ring oscillator system 400 may further include a ring oscillator bias circuit 450 coupled to the differential ring oscillator 410 and configured to receive a control voltage 430 and provide power to the inverters in the differential ring oscillator 410 in the form of an oscillator up voltage 452 and an oscillator down voltage 454.

In some embodiments, the differential ring oscillator 410 may include a number of inverters arranged to maintain and propagate an oscillation signal, along with the dummy section 440. The injection section 420 may be configured to receive an external signal (for example, the external signal 120), which may be represented as the injection current source 426 and voltages at the gates of the transistors 422 and 424, and may inject the external signal into the differential ring oscillator 410. The dummy section 440 may be configured to provide a common-mode signal to the differential ring oscillator 410 via the transistors 442 and 444 for differential operation. The ring oscillator bias circuit 450 may be configured to adjust the oscillator up voltage 452 and the oscillator down voltage 454 provided to the inverters in the differential ring oscillator 410 based on the control voltage 430 (for example, the control signal 330).

FIG. 5 illustrates a detailed diagram of an example ring oscillator system that may implement quadrature-based injection locking, arranged in accordance with at least some embodiments described herein.

As depicted in a ring oscillator system 500, a differential ring oscillator 520 (similar to the differential ring oscillator 410) may receive a differential external signal from a differential injection stage 510 coupled to a clock input 502. The clock input 502 may include a photodiode 504 configured to receive an optical clock signal 506. The injection stage 510 may include a transimpedance amplifier 512 coupled to a single-to-differential stage 514, and one of the output terminals of the injection stage 510 may be coupled to a common mode voltage 516. A differential quadrature phase detector 530 (similar to the phase detector 310) coupled to the differential ring oscillator 520 may measure quadrature output oscillation signals from the differential ring oscillator 520 and determine an MQE from the measured signals. The quadrature phase detector 530 may then send the MQE to a differential charge pump and filter 540, which may be implemented as a low-pass filter (similar to the low-pass filter 320).

In some embodiments, the clock input 502 may be configured to convert the optical clock signal 506 into an electrical clock signal using the photodiode 504. The clock input 502 may then provide the electrical clock signal to the injection stage 510 as an injection signal to be injected into the differential ring oscillator 520 (for example, the external signal 120). In some embodiments, the clock input 502 may provide the electrical clock signal as a time-varying current signal. The transimpedance amplifier 512 in the differential injection stage 510 may first convert the injection signal into an amplified time-varying voltage injection signal. The single-to-differential stage 514 may then convert the voltage injection signal into a differential signal suitable for the differential ring oscillator 520, then inject the differential injection signal into the differential ring oscillator 520.

The differential quadrature phase detector 530 may measure the phases of two quadrature oscillation signals output

by the differential ring oscillator **520** and convert the measured phases into the MQE, as described above. The differential charge pump and filter **540**, which may implement a low-pass filter using a charge pump, may then receive the MQE and generate a control signal V_{ctrl} **550** from the MQE by, for example, reducing the magnitude of high-frequency components of the MQE while maintaining the magnitude of low-frequency components of the MQE. The control signal V_{ctrl} **550** may then be used to adjust the supply voltage of the differential ring oscillator **520**, for example, via a bias circuit such as the ring oscillator bias circuit **450**.

FIG. **6** illustrates an example on-chip clock distribution system that may use quadrature-based injection locking, arranged in accordance with at least some embodiments described herein.

According to a diagram **600**, an on-chip clock distribution system **610** may include a quadrature-based injection-locked ring oscillator system **616** coupled to receive an optical clock signal **612** through an optical fiber **614**. The ring oscillator system **616** may convert the optical clock signal **612** into an electrical clock, signal using, for example, an injection stage similar to the injection stage **510**. The ring oscillator system **616** may then perform injection locking based on mean quadrature error as described above and output four quadrature output oscillation signals **618** (for example, the output oscillation signals **130-136**), each signal offset from the other signals by at least 90° in phase. The signals **618** may then be used to process incoming data. For example, the signals **618** may first be de-skewed to provide synchronization at de-skew stages **632**, **634**, **636** and **638**. The de-skewed signals may then be used to recover data **642**, **644**, **646**, and **648** from modulated/encoded data signals **622**, **624**, **626**, and **628** at data recovery stages **641**, **643**, **645**, and **647**, respectively.

FIG. **7** illustrates a general purpose computing device that could be used in conjunction with a ring oscillator that implements quadrature-based injection-locking, arranged in accordance with at least some embodiments described herein.

For example, the computing device **700** may be used to implement quadrature-based injection locking of ring oscillators as described herein, in one or more components of the computing device **700** that operate with clock signals. Alternatively or additionally, the computing device **700** may be used to control the operation of ring oscillators so as to implement quadrature-based injection locking, wherein such ring oscillators may be located within or external to the computing device **700**. In an example basic configuration **702**, the computing device **700** may include one or more processors **704** and a system memory **706**. A memory bus **708** may be used to communicate between the processor **704** and the system memory **706**. The basic configuration **702** is illustrated in FIG. **7** by those components within the inner dashed line.

Depending on the desired configuration, the processor **704** may be of any type, including but not limited to a microprocessor (μ P), a microcontroller (μ C), a digital signal processor (DSP), or any combination thereof. The processor **704** may include one more levels of caching, such as a cache memory **712**, a processor core **714**, and registers **716**. The example processor core **714** may include an arithmetic logic unit (ALU), a floating point unit (FPU), a digital signal processing core (DSP Core), or any combination thereof. An example memory controller **718** may also be used with the processor **704**, or in some implementations, the memory controller **718** may be an internal part of the processor **704**.

Depending on the desired configuration, the system memory **706** may be of any type including but not limited to volatile memory (such as RAM), non-volatile memory (such as ROM, flash memory, etc.) or any combination thereof. The system memory **706** may include an operating system **720**, a control module **722**, and program data **724**. The control module **722** may include a phase detector module **726** and a mean quadrature error module **728** to implement or otherwise control operations associated with quadrature-based ring oscillator injection locking as described herein.

The computing device **700** may have additional features or functionality, and additional interfaces to facilitate communications between the basic configuration **702** and any desired devices and interfaces. For example, a bus/interface controller **730** may be used to facilitate communications between the basic configuration **702** and one or more data storage devices **732** via a storage interface bus **734**. The data storage devices **732** may be one or more removable storage devices **736**, one or more non-removable storage devices **738**, or a combination thereof. Examples of the removable storage and the non-removable storage devices include magnetic disk devices such as flexible disk drives and hard-disk drives (HDDs), optical disk drives such as compact disk (CD) drives or digital versatile disk (DVD) drives, solid state drives (SSDs), and tape drives to name a few. Example computer storage media may include volatile and non-volatile, removable and non-removable media implemented in any method or technology for storage of information, such as computer readable instructions, data structures, program modules, or other data.

The system memory **706**, the removable storage devices **736** and the non-removable storage devices **738** are examples of computer storage media. Computer storage media includes, but is not limited to, RAM, ROM, EEPROM, flash memory or other memory technology, CD-ROM, digital versatile disks (DVDs), solid state drives, or other optical storage, magnetic cassettes, magnetic tape, magnetic disk storage or other magnetic storage devices, or any other medium which may be used to store the desired information and which may be accessed by the computing device **700**. Any such computer storage media may be part of the computing device **700**.

The computing device **700** may also include an interface bus **740** for facilitating communication from various interface devices (e.g., one or more output devices **742**, one or more peripheral interfaces **744**, and one of more communication devices **766**) to the basic configuration **702** via the bus/interface controller **730**. Some of the example output devices **742** include a graphics processing unit **748** and an audio processing unit **750**, which may be configured to communicate to various external devices such as a display or speakers via one or more A/V ports **752**. One or more example peripheral interfaces **744** may include a serial interface controller **754** or a parallel interface controller **756**, which may be configured to communicate with external devices such as input devices (e.g., keyboard, mouse, pen, voice input device, touch input device, etc.) or other peripheral devices (e.g., printer, scanner, etc.) via one or more I/O ports **758**. An example communication device **766** includes a network controller **760**, which may be arranged to facilitate communications with one or more other computing devices **762** over a network communication link via one or more communication ports **764**.

The network communication link may be one example of a communication media. Communication media may be embodied by computer readable instructions, data structures, program modules, or other data in a modulated data

signal, such as a carrier wave or other transport mechanism, and may include any information delivery media. A “modulated data signal” may be a signal that has one or more of its characteristics set or changed in such a manner as to encode information in the signal. By way of example, and not limitation, communication media may include wired media such as a wired network or direct-wired connection, and wireless media such as acoustic, radio frequency (RF), microwave, infrared (IR) and other wireless media. The term computer readable media as used herein may include both storage media and communication media.

The computing device **700** may be implemented as a part of a general purpose or specialized server, mainframe, or similar computer that includes any of the above functions or features. The computing device **700** may also be implemented as a personal computer including both laptop computer and non-laptop computer configurations.

FIG. **8** is a flow diagram illustrating an example method to perform quadrature-based injection-locking of a ring oscillator that may be performed by a computing device such as the computing device in FIG. **7**, arranged in accordance with at least some embodiments described herein.

Example methods may include one or more operations, functions or actions as illustrated by one or more of blocks **822**, **824**, **826**, **828**, and/or **830**, and may in some embodiments be performed (or otherwise controlled) by and/or in a computing device such as the computing device **800** in FIG. **8**. The operations described in the blocks **822-830** may also be stored as computer-executable instructions in a computer-readable medium such as a computer-readable medium **820** of a computing device **810**.

An example process for implementing quadrature-based injection locking of ring oscillators may begin with block **822** “INJECT EXTERNAL SIGNAL WITH FREQUENCY F_{inj} INTO RING OSCILLATOR WITH NATURAL FREQUENCY F_0 ”, where an injection stage (for example, the injection stage **510**) may inject an external signal such as a clock signal having a frequency f_{inj} into a ring oscillator (for example, the ring oscillator **100**) that may have a different natural frequency f_0 , as described above.

Block **822** may be followed by block **824**, “MEASURE PHASE SIGNALS RESULTING FROM THE COUPLING OF F_{inj} AND F_0 FROM MULTIPLE INVERTERS IN THE RING OSCILLATOR”, where a phase detector module (for example, the phase detector **310**) may measure the phases of quadrature signals (for example, the output oscillation signals **130** and **134**) output from the ring oscillator, as described above. The frequencies and phases of the quadrature signals may result from the coupling of the external signal having the frequency f_{inj} and the natural frequency f_0 of the ring oscillator.

Block **824** may be followed by block **826**, “DETERMINE MEAN QUADRATURE ERROR (MQE) FROM MEASURED PHASE SIGNALS”, where the phase detector module may determine a mean quadrature error (MQE) parameter as described above from the quadrature signal phases measured at block **824**. In some embodiments, the MQE parameter may vary directly with the difference between the measured quadrature signal phases.

Block **826** may be followed by block **828**, “GENERATE CONTROL SIGNAL FROM DETERMINED MQE”, where a low-pass filter (for example, the low-pass filter **320**) may generate a control signal (for example, the control signal **330**) as described above from the MQE determined at block **826**. In some embodiments, the control signal may include relatively low frequency components of the MQE, generated by passing the MQE through a low-pass filter.

Block **828** may be followed by block **830**, “ADJUST SUPPLY VOLTAGE OF INVERTERS IN RING OSCILLATOR BASED ON GENERATED CONTROL SIGNAL”, where the control signal may be used to adjust the supply voltage of one or more inverters (for example, the inverters **102-108**) in the ring oscillator to reduce the difference between the f_{inj} of the external signal and the natural frequency f_0 of the ring oscillator, as described above. In some embodiments, the control signal itself may be used as the supply voltage value.

FIG. **9** illustrates a block diagram of an example computer program product, arranged in accordance with at least some embodiments described herein.

In some examples, as shown in FIG. **9**, a computer program product **900** may include a signal bearing, medium **902** that may also include one or more machine readable instructions **904** that, in response to execution by, for example, a processor may provide the functionality and features described herein. Thus, for example, referring to the processor **704** in FIG. **7**, the control module **722** may undertake one or more of the tasks shown FIG. **9** in response to the instructions **904** conveyed to the processor **704** by the medium **902** to perform/control actions associated with quadrature-based injection locking of ring oscillators as described herein. Some of those instructions may include, for example, instructions to inject an external signal with frequency f_{inj} into a ring oscillator with natural frequency f_0 , measure phase signals resulting from the coupling of f_{inj} and f_0 from multiple inverters in the ring oscillator, determine mean quadrature error (MQE) from the measured phase signals, generate a control signal from the determined MQE, and/or adjust the supply voltage(s) of inverters in the ring oscillator based on the generate control signal, according to some embodiments described herein.

In some implementations, the signal bearing media **902** depicted in FIG. **9** may encompass computer-readable media **906**, such as, but not limited to, a hard disk drive, a solid state drive, a compact disk (CD), a digital versatile disk (DVD), a digital tape, memory, etc. In some implementations, the signal bearing media **902** may encompass recordable media **907**, such as, but not limited to, memory, read/write (R/W) CDs, R/W DVDs, etc. In some implementations, the signal bearing media **902** may encompass communications media **910**, such as, but not limited to, a digital and/or an analog communication medium (e.g. a fiber optic cable, a waveguide, a wired communications link, a wireless communication link, etc.). Thus, for example, the program product **900** may be conveyed to one or more modules of the processor **704** by an RF signal bearing medium, where the signal bearing media **902** is conveyed by the wireless communications media **910** (e.g., a wireless communications medium conforming with the IEEE 802.11 standard).

According to some examples, methods are described to injection-lock a ring oscillator having multiple inverters and a natural frequency. Example methods may include injecting an external signal with an injection frequency into the multiple inverters, detecting a first phase signal, formed from a coupling of the natural frequency and the injection frequency, from a first inverter in the multiple inverters. The methods may also include detecting a second phase signal, formed from the coupling of the natural frequency and the injection frequency, from a second inverter in the multiple inverters, determining a mean quadrature error (MQE) from at least the first phase signal and the second phase signal. The methods may further include generating a control signal

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from the determined MQE and adjusting the natural frequency of the ring oscillator based on the control signal.

According to some embodiments, injecting the external signal may include injecting the external signal into an input terminal of the first inverter. Generating the control signal may include generating the control signal from the MQE by use of a low-pass filter. Adjusting the natural frequency of the ring oscillator may include adjusting the natural frequency so as to reduce a magnitude of the MQE. Adjust the natural frequency may further include increasing the natural frequency in response to the determined MQE being greater than zero and decreasing the natural frequency in response to the determined MQE being less than zero. Adjusting the natural frequency may include adjusting the natural frequency using adjusting of a supply voltage to at least one of the multiple inverters based on the control signal. The method may further include using the control signal as the supply voltage.

According to other examples, injection-locked ring-oscillator systems are described. Example systems may include multiple inverters, a phase detector module coupled to the multiple inverters, and a control module coupled to the phase detector module. The inverters may be configured to receive an external signal with an injection frequency and to output an oscillation signal. The phase detector module may be configured to detect a first phase signal, formed from a coupling of a natural frequency of the system and the injection frequency, from a first inverter in the multiple inverters and to detect a second phase signal, formed from the coupling of the natural frequency of the system and the injection frequency from a second inverter in the multiple inverters. The phase detector module may also be configured to determine a mean quadrature error (MQE) from at least the first phase signal and the second phase signal. The control module may be configured to generate a control signal from the determined MQE and adjust a supply voltage to at least one of the multiple inverters based on the control signal.

According to some embodiments, the multiple inverters may be configured to receive the external signal at an input terminal of the first inverter. The control module may include a low-pass filter and may be configured to generate the control signal from the determined MQE by use of the low-pass filter. The low-pass filter may include a charge pump. The control module may be configured to adjust the supply voltage so as to reduce a magnitude of the MQE.

According to other embodiments, the control module may be configured to increase a magnitude of the control signal in response to the determined MQE being greater than zero and decrease the magnitude of the control signal in response to the determined MQE being less than zero. The supply voltage may include the control signal, and the multiple inverters may be configured to implement a quadrature ring oscillator.

According to further examples, a clock signal distribution circuit is provided. The circuit may include a clock signal injection state, a ring oscillator with a natural frequency and coupled to the clock signal injection stage, a quadrature phase detector module coupled to the ring oscillator, and a low-pass filter module coupled to the ring oscillator and the quadrature phase detector module. The clock signal injection stage may be configured to receive a clock signal and use the clock signal to output an injection signal with an injection frequency. The ring oscillator may be configured to receive the injection signal and output multiple oscillation signals. The quadrature phase detector module may be configured to detect, from the ring oscillator, multiple phase

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signals formed from the coupling of the natural frequency and the injection frequency, and determine a mean quadrature error (MQE) from the multiple phase signals. The low-pass filter module may be configured to generate a control signal from the determined MQE and provide the control signal to the ring oscillator.

According to some embodiments, the clock signal may include an optical signal, the injection signal may include an electrical signal, and the clock signal injection stage may be further configured to convert the optical signal into the electrical signal. The low-pass filter module may include a charge pump, and/or may be configured to provide the control signal to the ring oscillator so as to reduce a magnitude of the MQE. The low-pass filter module may be configured to increase a magnitude of the control signal in response to the determined MQE being greater than zero and decrease the magnitude of the control signal in response to the determined MQE being less than zero.

According to other embodiments, the low-pass filter module may be configured to provide the control signal to the ring oscillator as a supply voltage equivalent to the control signal. The clock signal injection stage, the ring oscillator, the quadrature phase detector module, and the low-pass filter module may be configured to operate in a differential manner. The multiple oscillation signal may include quadrature signals to be distributed to data processor blocks.

Various embodiments may be implemented in hardware, software, or combination of both hardware and software (or other computer-readable instructions stored on a non-transitory computer-readable storage medium and executable by one or more processors); the use of hardware or software is generally (but not always, in that in certain contexts the choice between hardware and software may become significant) a design choice representing cost vs. efficiency tradeoffs. There are various vehicles by which processes and/or systems and/or other technologies described herein may be effected (e.g., hardware, software, and/or firmware), and the preferred vehicle will vary with the context in which the processes and/or systems and/or other technologies are deployed. For example, if an implementer determines that speed and accuracy are paramount, the implementer may opt for a mainly hardware and/or firmware vehicle; if flexibility is paramount, the implementer may opt for a mainly software implementation; or, yet again alternatively, the implementer may opt for some combination of hardware, software, and/or firmware.

The foregoing detailed description has set forth various embodiments of the devices and/or processes via the use of block diagrams, flowcharts, and/or examples. Insofar as such block diagrams, flowcharts, and/or examples contain one or more functions and/or operations, each function and/or operation within such block diagrams, flowcharts, or examples may be implemented, individually and/or collectively, by a wide range of hardware, software, firmware, or virtually any combination thereof. In one embodiment, several portions of the subject matter described herein may be implemented via application specific integrated circuits (ASICs), field programmable gate arrays (FPGAs), digital signal processors (DSPs), or other integrated formats. However, some aspects of the embodiments disclosed herein, in whole or in part, may be equivalently implemented in integrated circuits, as one or more computer programs executing on one or more computers (e.g., as one or more programs executing on one or more computer systems), as one or more programs executing on one or more processors (e.g., as one or more programs executing on one or more microprocessors), as firmware, or as virtually any combina-

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tion thereof, and designing the circuitry and/or writing the code for the software and/or firmware are possible in light of this disclosure.

The present disclosure is not to be limited in terms of the particular embodiments described in this application, which are intended as illustrations of various aspects. Many modifications and variations can be made without departing from its spirit and scope. Functionally equivalent methods and apparatuses within the scope of the disclosure, in addition to those enumerated herein, are possible from the foregoing descriptions. Such modifications and variations are intended to fall within the scope of the appended claims. The present disclosure is to be limited only by the terms of the appended claims, along with the full scope of equivalents to which such claims are entitled. Also, the terminology used herein is for the purpose of describing particular embodiments only, and is not intended to be limiting.

In addition, the mechanisms of the subject matter described herein are capable of being distributed as a program product in a variety of forms, and that an illustrative embodiment of the subject matter described herein applies regardless of the particular type of signal bearing medium used to actually carry out the distribution. Examples of a signal bearing medium include, but are not limited to, the following: a recordable type medium such as a floppy disk, a hard disk drive, a compact disc (CD), a digital versatile disk (DVD), a digital tape, a computer memory, a solid state drive, etc.; and a transmission type medium such as a digital and/or an analog communication medium (e.g., a fiber optic cable, a waveguide, a wired communications link, a wireless communication link, etc.).

Those skilled in the art will recognize that it is common within the art to describe devices and/or processes in the fashion set forth herein, and thereafter use engineering practices to integrate such described devices and/or processes into data processing systems. That is, at least a portion of the devices and/or processes described herein may be integrated into a data processing system via a reasonable amount of experimentation. A data processing system may include one or more of a system unit housing, a video display device, a memory such as volatile and non-volatile memory, processors such as microprocessors and digital signal processors, computational entities such as operating systems, drivers, graphical user interfaces, and applications programs, one or more interaction devices, such as a touch pad or screen, and/or control systems including feedback loops and control motors e.g., control motors to move and/or adjust components and/or quantities).

A data processing system may be implemented utilizing any suitable commercially available components, such as those found in data computing/communication and/or network computing/communication systems. The herein described subject matter sometimes illustrates different components contained within, or connected with, different other components. Such depicted architectures are merely exemplary, and in fact many other architectures may be implemented which achieve the same functionality. In a conceptual sense, any arrangement of components to achieve the same functionality is effectively "associated" such that the desired functionality is achieved. Hence, any two components herein combined to achieve a particular functionality may be seen as "associated with" each other such that the desired functionality is achieved, irrespective of architectures or intermediate components. Likewise, any two components so associated may also be viewed as being "operably connected", or "operably coupled", to each other to achieve the desired functionality, and any two compo-

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nents capable of being so associated may also be viewed as being "operably couplable", to each other to achieve the desired functionality. Specific examples of operably couplable include but are not limited to physically connectable and/or physically interacting components and/or wirelessly interactable and/or wirelessly interacting components and/or logically interacting and/or logically interactable components.

With respect to the use of substantially any plural and/or singular terms herein, those having skill in the art can translate from the plural to the singular and/or from the singular to the plural as is appropriate to the context and/or application. The various singular/plural permutations may be expressly set forth herein for sake of clarity.

It will be understood by those within the art that, in general, terms used herein, and especially in the appended claims (e.g., bodies of the appended claims) are generally intended as "open" terms (e.g., the term "including" should be interpreted as "including but not limited to," the term "having" should be interpreted as "having at least," the term "includes" should be interpreted as "includes but is not limited to," etc.). It will be further understood by those within the art that if a specific number of an introduced claim recitation is intended, such an intent will be explicitly recited in the claim, and in the absence of such recitation no such intent is present. For example, as an aid to understanding, the following appended claims may contain usage of the introductory phrases "at least one" and "one or more" to introduce claim recitations. However, the use of such phrases should not be construed to imply that the introduction of a claim recitation by the indefinite articles "a" or "an" limits any particular claim containing such introduced claim recitation to embodiments containing only one such recitation, even when the same claim includes the introductory phrases "one or more" or "at least one" and indefinite articles such as "a" or "an" (e.g., "a" and/or "an" should be interpreted to mean "at least one" or "one or more"); the same holds true for the use of definite articles used to introduce claim recitations. In addition, even if a specific number of an introduced claim recitation is explicitly recited, those skilled in the art will recognize that such recitation should be interpreted to mean at least the recited number (e.g., the bare recitation of "two recitations," without other modifiers, means at least two recitations, or two or more recitations).

Furthermore, in those instances where a convention analogous to "at least one of A, B, and C, etc." is used, in general such a construction is intended in the sense one having skill in the art would understand the convention (e.g., "a system having at least one of A, B, and C" would include but not be limited to systems that have A alone, B alone, C alone, A and B together, A and C together, B and C together, and/or A, B, and C together, etc.). It will be further understood by those within the art that virtually any disjunctive word and/or phrase presenting two or more alternative terms, whether in the description, claims, or drawings, should be understood to contemplate the possibilities of including one of the terms, either of the terms, or both terms. For example, the phrase "A or B" will be understood to include the possibilities of "A" or "B" or "A and B."

As will be understood by one skilled in the art, for any and all purposes, such as in terms of providing a written description, all ranges disclosed herein also encompass any and all possible subranges and combinations of subranges thereof. Any listed range can be easily recognized as sufficiently describing and enabling the same range being broken down into at least equal halves, thirds, quarters, fifths, tenths, etc.

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As a non-limiting example, each range discussed herein can be readily broken down into a lower third, middle third and upper third, etc. As will also be understood by one skilled in the art all language such as “up to,” “at least,” “greater than,” “less than,” and the like include the number recited and refer to ranges which can be subsequently broken down into subranges as discussed above. Finally, as will be understood by one skilled in the art, a range includes each individual member. Thus, for example, a group having 1-3 cells refers to groups having 1, 2, or 3 cells. Similarly, a group having 1-5 cells refers to groups having 1, 2, 3, 4, or 5 cells, and so forth.

While various aspects and embodiments have been disclosed herein, other aspects and embodiments are possible. The various aspects and embodiments disclosed herein are for purposes of illustration and are not intended to be limiting, with the true scope and spirit being indicated by the following claims.

What is claimed is:

1. An injection-locked ring oscillator system, comprising:
 - a plurality of inverters configured to receive an external signal with an injection frequency;
 - a phase detector module coupled to the plurality of inverters, wherein the phase detector module is configured to:
 - detect a first phase signal, formed from a coupling of a natural frequency of the injection-locked ring oscillator system and the injection frequency, from a first inverter of the plurality of inverters;
 - detect a second phase signal, formed from the coupling of the natural frequency and the injection frequency, from a second inverter of the plurality of inverters;
 - detect a mismatch between the injection frequency and the natural frequency; and
 - identify phase errors in the first phase signal and the second phase signal based on the mismatch; and
 - a control module coupled to the phase detector module, wherein the control module is configured to:
 - generate control signal based on the phase errors, wherein the control signal is configured to control the injection-locked ring oscillator system.
2. The injection-locked ring oscillator system of claim 1, wherein the control signal is configured to adjust the natural frequency to reduce a difference between the natural frequency and the injection frequency.
3. The injection-locked ring oscillator system of claim 1, wherein at least one of the plurality of inverters is configured to output oscillation signal, and wherein the phase detector module is further configured to:
 - reduce phase errors in the oscillation signal by a reduction of a frequency difference between the injection frequency and the natural frequency.
4. The injection-locked ring oscillator system of claim 1, wherein the phase detector module is further configured to:
 - determine a mean quadrature error (MQE) from at least the first phase signal and the second phase signal, wherein the MQE is usable to generate the control signal to control the injection-locked ring oscillator system.
5. The injection-locked ring oscillator system of claim 4, wherein the MQE includes an average quadrature phase error, and wherein the average quadrature phase error includes a phase difference between the first phase signal and the second phase signal.

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6. The injection-locked ring oscillator system of claim 5, wherein the MQE is determined by:

$$MQE = \frac{\pi}{2} \left(\frac{\omega_{inj}}{\omega_0} + \frac{\omega_b}{\omega_0} - 1 \right), \text{ where}$$

$$\omega_{inj} = 2\pi f_{inj},$$

$$\omega_0 = 2\pi f_0,$$

$$\omega_b = \sqrt{(\omega_0 - \omega_{inj})^2 - \omega_l^2}, \text{ and}$$

$$\omega_l = \frac{\omega_0}{2Q}k, \text{ where}$$

f_{inj} is a measurement of the injection frequency and is 15 gigahertz (GHz), f_0 is a measurement of the natural frequency GHz, $k=0.2$, and $Q=1.25$.

7. The injection-locked ring oscillator system of claim 6, wherein the phase detector module is further configured to:

- detect a locked state of the injection-locked ring oscillator system, wherein the locked state includes

$$(\omega_0 - \omega_{inj})^2 < \omega_l^2; \text{ and}$$

reduce the phase errors in an oscillation signal by an adjustment of a value of f_0 until a value of the MQE is substantially zero, wherein the value of the MQE is substantially zero when the value of f_0 equals a value of f_{inj} .

8. The injection-locked ring oscillator system of claim 6, wherein the phase detector module is further configured to:

- compare a value of f_0 to a value of f_{inj} ;
- determine the value of f_0 as being less than the value of f_{inj} ; and
- in response to a determination that the value of f_0 is less than the value of f_{inj} , identify a positive value of the MQE.

9. The injection-locked ring oscillator system of claim 8, further comprising a low-pass filter module coupled to the phase detector module, wherein the phase detector module is further configured to:

- transmit the MQE to the low-pass filter module, wherein the low-pass filter module is configured to:
 - increase a magnitude of the control signal; and
 - increase a supply voltage to at least one of the plurality of inverters based on the magnitude of the control signal, wherein the increase in the supply voltage increases the value of f_0 .

10. The injection-locked ring oscillator system of claim 6, wherein the phase detector module is further configured to:

- compare a value of f_0 to a value of f_{inj} ;
- determine the value of f_0 as being greater than the value of f_{inj} ; and
- in response to a determination that the value of f_0 is greater than the value of f_{inj} , identify a negative value of the MQE.

11. The injection-locked ring oscillator system of claim 10, further comprising a low-pass filter module coupled to the phase detector module, wherein the phase detector module is further configured to:

- transmit the MQE to the low-pass filter module, wherein the low-pass filter module is configured to:
 - decrease a magnitude of the control signal; and
 - decrease a supply voltage to at least one of the inverters of the plurality of inverters based on the magnitude of the control signal, wherein the decrease in the supply voltage decreases the value of f_0 .

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12. A clock signal distribution circuit, comprising:
 a clock signal injection stage, wherein the clock signal injection stage is configured to:
 receive a clock signal; and
 use the clock signal to output an injection signal with an injection frequency;
 a ring oscillator with a natural frequency and coupled to the clock signal injection stage, wherein the ring oscillator configured to
 receive the injection signal; and
 output oscillation signals; and
 a quadrature phase detector module coupled to the ring oscillator, wherein the quadrature phase detector module is configured to:
 detect, from the ring oscillator, phase signals formed from a coupling of the natural frequency and the injection frequency; and
 determine a mean quadrature error (MQE) from the phase signals, wherein the MQE is usable to generate a control signal to control the ring oscillator.
13. The clock signal distribution circuit of claim 12, wherein the clock signal includes an optical clock signal.
14. The clock signal distribution circuit of claim 13, wherein the clock signal injection stage is further configured to:
 convert the optical clock signal into an electrical clock signal using a photodiode.
15. The clock signal distribution circuit of claim 14, wherein the clock signal injection stage is further configured to:
 provide the electrical clock signal as a time-varying current signal to the ring oscillator.
16. The clock signal distribution circuit of claim 12, wherein a first oscillation signal of the oscillation signals is offset by at least 90° relative to a second oscillation signal of the oscillation signals.

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17. A method to injection-lock a ring oscillator that includes a plurality of inverters and a natural frequency, the method comprising:
 injecting an external signal with an injection frequency into at least one of the plurality of inverters;
 detecting a first phase signal, formed from a coupling of the natural frequency and the injection frequency, from a first inverter in the plurality of inverters;
 detecting a second phase signal, formed from the coupling of the natural frequency and the injection frequency, from a second inverter in the plurality of inverters;
 detecting a mismatch between the injection frequency and the natural frequency;
 identifying, phase errors in the first phase signal and the second phase signal based on the mismatch; and
 generating a control signal based on the phase errors, wherein the control signal is configured to control the ring oscillator.
18. The method of claim 17, further comprising:
 reducing the phase errors in the first phase signal and the second phase signal by a reduction of a difference between the frequency of the external signal and the natural frequency.
19. The method of claim 17, further comprising:
 determining a mean quadrature error (MQE) from at least the first phase signal and the second phase signal, wherein the MQE is usable to generate the control signal to control the ring oscillator.
20. The method of claim 19, further comprising:
 adjusting the natural frequency of the ring oscillator to reduce a magnitude of the MQE by one of:
 increasing the natural frequency in response to a detection of a value of the MQE as being greater than zero; and
 decreasing the natural frequency in response to the detection of the value of the MQE as being less than zero.

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